



A UNIFIED FRAMEWORK FOR COLLECTIVE SYSTEMS

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Grand Vision

Applications



A Software Toolkit of
Design Patterns and
Components



A Unified Theory of
Operations for CAST
Systems



Why do we need a new theory ?

- Existing engineering approaches provide some theoretical basis
 - E.g. control theory – ensure/prove stability
- But most methods don't account for defining properties of CAST systems
 - Lead to systems that are oscillatory or at worst unfit for purpose
- Existing methods often domain-driven (e.g. telecoms, robotics)
 - Not generalisable or transferable

Diverse objectives

noisy

distributed

heterogeneous

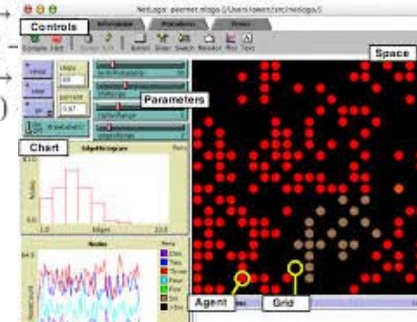
open

dynamic

CAS is Multi-Disciplinary

- Many theories from individual disciplines
- Hard to compare theories
- Theories address different aspects of CAS
- Don't account for engineering constraints

- (MTL1): $(A \rightarrow B) \rightarrow ((B \rightarrow C) \rightarrow (A \rightarrow C))$
- (MTL2): $A \otimes B \rightarrow A$
- (MTL3): $A \otimes B \rightarrow B \otimes A$
- (MTL4a): $A \wedge B \rightarrow A$
- (MTL4b): $A \wedge B \rightarrow B \wedge A$
- (MTL4c): $A \otimes (A \rightarrow B) \rightarrow B$
- (MTL5a): $(A \rightarrow (B \rightarrow C)) \rightarrow (A \rightarrow B) \rightarrow C$
- (MTL5b): $(A \otimes B) \rightarrow (A \rightarrow B)$
- (MTL6): $((A \rightarrow B) \rightarrow C) \rightarrow (A \rightarrow (B \rightarrow C))$
- (MTL7): \perp

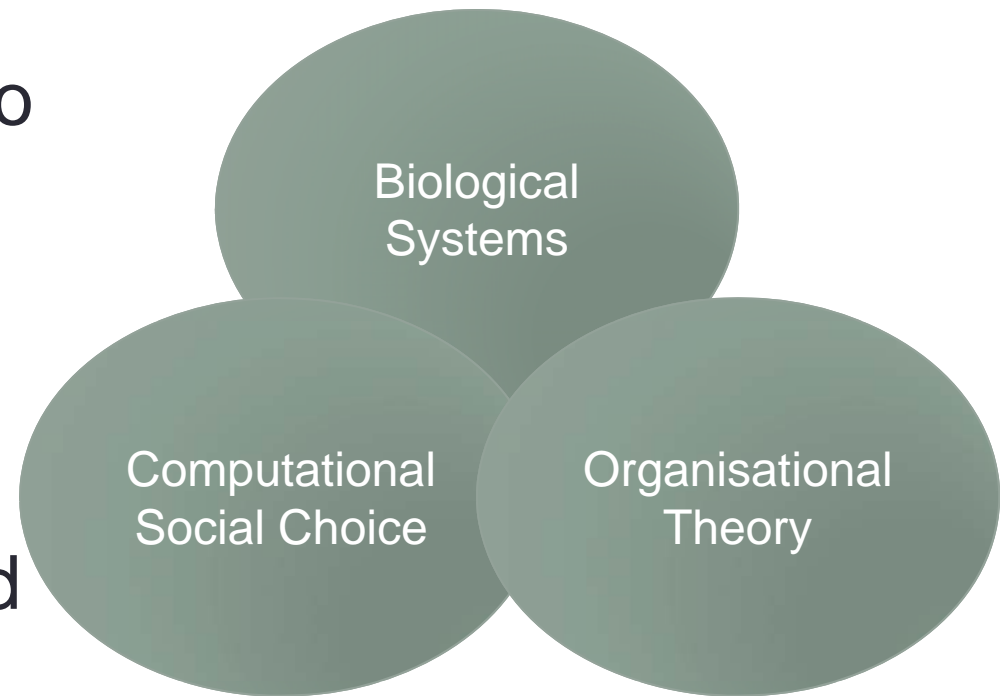


$$\begin{aligned}
 (x')^2 + x^2 &= 4 \\
 \left(\frac{dx}{dt}\right)^2 + x^2 &= 4 \\
 \frac{dx}{dt} &= (4 - x^2)^{\frac{1}{2}} \\
 \frac{dx}{(4 - x^2)^{\frac{1}{2}}} &= dt \\
 \int (4 - x^2)^{-\frac{1}{2}} dx &= \int dt \\
 \sin^{-1}\left(\frac{x}{2}\right) &= t + C \\
 \frac{x}{2} &= \sin t \\
 x &= 2 \sin t
 \end{aligned}$$



Towards a unified theory

- Unifies concepts from multiple disciplines into a single framework
- Qualitative theory represented in axiomatic form
- Can be formalised and analysed
- Operationalised via design patterns



Biological Systems

- Immune-neuro-endocrine mechanisms lead to *homeostasis*
 - Cohen's cognitive immune system :
 - Decision making via co-responsence
 - Swarm insects
 - Coordination, partial info
 - Symbiosis between multiple species:
 - Cooperation
- *Long-term stability*
 - *Adapt over multiple timescales*
 - *Coordinate multiple heterogeneous components*
 - *Deal with limited and partial information*
 - *Decision making*
 - *Conflict resolution*

Social Choice Theory

- Originates in *economics* and *political science*
 - Concerns design & analysis of methods for aggregating preferences of multiple agents into collective decisions
 - Social choice considers formal aspects of democratic decision making (e.g electoral systems)
 - *Computational* Social Choice add an algorithmic perspective
- Heterogeneous agents
 - Multiple objectives
 - Collective decisions
 - Open-ness
 - Fair division of resources
 - Stability

Organisational Theory

- Elucidates principles for stable resource management
- Study of engineered systems
- Insights into engineering socio-technical 'organisations' in a top down manner

- Collective Action
- Trust
- Cooperation
- Stable and enduring systems

A Unified Theory of Operation

A Unified Theory of Operations for CAST Systems

Computational
Social Choice

Biological
Systems

Organisational
Theory

Open-ness

Noisy Information

Social Interactions

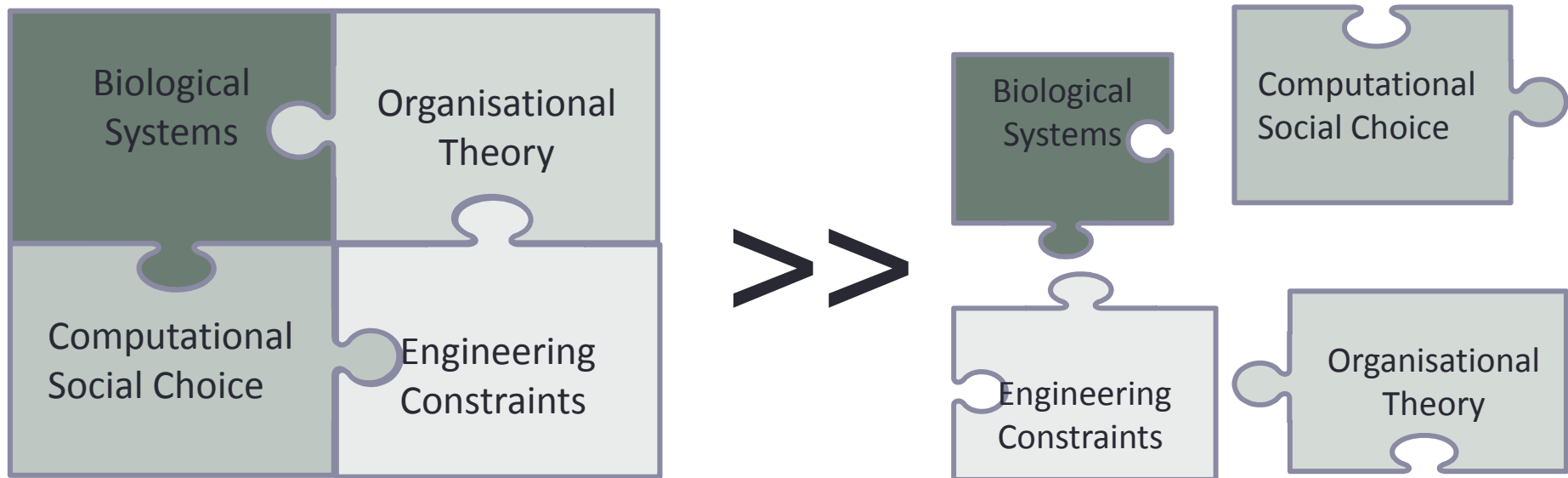
Conflicts

Diverse Objectives

New CAST properties...

Engineering Requirements of CAST Systems

What does synthesis give ?



- Addresses weaknesses in individual theories
- Addresses conflicts
- Respects engineering constraints

Individual Weaknesses

- **Biological Systems:**
 - Tend to rely on homogeneous collectives
 - Global rather than individual objectives
 - Considerable physical differences
- **Computational Social Choice**
 - Based on standard models from economics
 - Abstracted from human decision making (different goals but same model)
- **Institutional Theories**
 - Easy to get locked into sub-optimal states due to path dependencies
 - Not clear how to evaluate 'fitness' of an institution

Conclusions

- Unification addresses current fragmented approach to inter-disciplinary research
- Different analysis tools currently hinder elucidating connections between fields
- Many existing theories don't account for engineering constraints of CAS
- A unified theory will:
 - Enable formal comparison between concepts from different disciplines
 - Drive innovation in field